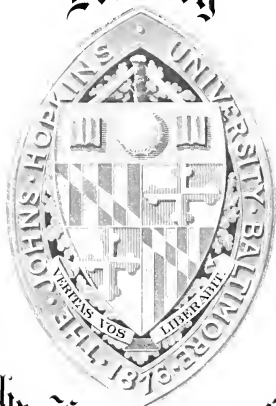


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ON THE ANALYSIS OF CERTAIN SPECTRUM LINES.

It is well-known that a change is produced in the wavelength and distribution of light in the lines of the spectrum of metallic vapours and gases when different external conditions are introduced. In most cases these changes were first observed and measured by means of the Rowland grating. Recently, however, these effects have become more readily observable through interference methods, in which the interference-roads are produced with large differences in the paths of the rays.

Michelson, by aid of his interferometer, resolved the important lines in the radiations of some vapours and gases rendered luminous in vacuum-tubes, and he has studied these radiations in a magnetic field. With his echelon spectroscope he has investigated the same subjects. Fabry and Perot with their interferometer have investigated the radiations from vapours in the electric arc and in vacuum-

* Phil. Mag. (5) 31, 337, 1891; 34, 250, 1892.

** Ann. de Chim. et Phys. 13, 189, 1876; 14, 11, 1877, 1878.
Astronom. Journ. 9, 27, 1899.

tures, and have applied their method for an exact determination of the wave-lengths of some of the lines in the spectrum of the iron arc and of the dark lines in the sun's spectrum. Lummer also by an interference method has studied the same radiations, particularly those from mercury, and has separated its prominent lines into many components.

When one compares the results of these investigations the agreement is not very satisfactory. Not only do the number and intensity of the components differ, but the distances between the components do not agree.

The work presented in this paper was undertaken at the suggestion of Professor Ames. The objects of the work were; to study interferometer methods; to obtain, if possible, more consistent results as to the constitution of the lines; and to determine the changes produced in the components under various conditions. Michelson remarks in one of the papers cited, "Still, in many cases, the range of visibility due to slight variations in the conditions shows that the behaviour of each substance must be carefully studied under all possible circumstances of temperature, pressure, strength of current, size and nature of electrodes, diameter of vacuum-tube, etc."

* Verh. d. Phys. Ges. 3, 1, 1901.
Zool. Zeit., (3), 1, 1901, 1902.

After experimenting a few weeks with both the Michelson and the Fabry and Perot interferometer the author was fully convinced that the Fabry and Perot method possessed the advantage for the problems in view, since it shows directly the structure of a given radiation by the simple inspection of the system of fringes. Each fringe is in fact a true spectrum of the source and the conditions are the same as those existing in the spectra obtained by the use of a grating having a small number of lines but where the spectra employed are of a very high order. During the progress of the experiments the method proposed by Lummer appeared. While I have not been able to use this method exactly, I used, before I read his paper, one which is very similar to it. This method and results obtained will be described below.

METHOD.

The method involved in this production of interference-fringes will be first briefly considered as it will assist towards a clear conception of the results.

Consider a ray of monochromatic light incident at an angle θ upon two glass plates whose inside surfaces (see Fig. 1), are slightly silvered and separated from one another a distance D . If the silvered surfaces are parallel, we have

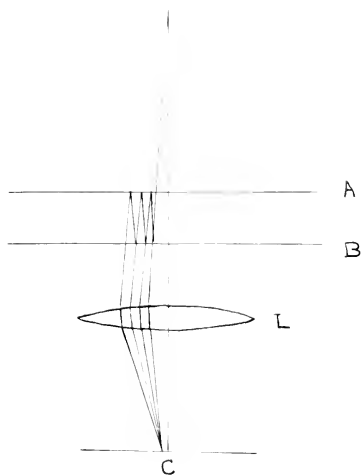


Fig. 1.

be parallel to the normal, it is reflected as a spherical wave-
front, rays coming from a point source, whose difference in
path increase in arithmetic progression. The dif-
ference of path between the first are $2f \cos \theta$,
 $4f \cos \theta$, ..., $2n f \cos \theta$. By means of a lens, the rays
are brought to a focus in its focal plane, producing
there an interference pattern, bright and dark bands ac-
cording as $2 f \cos \theta$, $4 f \cos \theta$, ... are equal to an even or
odd number of half wave-lengths. If we have a symmetrical
system of rays incident upon the plates, the system of fringes
obtained on a screen placed in the focal plane of the lens
will be concentric circles, having as their centre the
point of intersection of the normal from the source upon
the plates with the screen \mathcal{N} , in the figure. The radii of
these circles are equal to $f \tan \theta$, where f is the focal
length of the lens L .

The intensity of the light at different points of the
interference pattern was first worked out by Airy*. His
formula is

$$I = I_0 \left(\frac{1 - \frac{r^2}{r_0^2}}{1 - r^2} \right)^2 \sin^2 \left(\frac{\pi}{\lambda} \right)$$

where I_0 is the intensity of the incident light and r is the
amplitude ratio of the reflected and transmitted waves.

* Phil. Mag. (3) 2, 30, 1835.

where Δ is the path difference between the two rays.

It is now easy to see that the intensity of the light is a maximum when Δ is an even multiple of λ .

We see from this formula that for a given value of b , the intensity will have a maximum when $\frac{\Delta}{\lambda}$ is an even integer and a minimum when $\frac{\Delta}{\lambda}$ is an odd integer.

Hence the intensity of the light fringes is 1, while that of the dark fringes is 0. The intensity of the light fringes is 1, while that of the dark fringes is 0.

$$I = \left(\frac{1}{1 + \frac{b^2}{\lambda^2}} \right)^2.$$

Fairy and Perot have calculated the values of I for different values of b and have plotted curves showing the relation between I and Δ for these values of b . The greater the value of b the steeper becomes the intensity curve, so that the interference pattern consists of brighter fringes which are very narrow compared with the dark ones (see Plate 1, fig. 1). As we shall see later, the sharper and finer these bright bands are the easier are the radiation analyses and the components measured, thus, while on this account it is advantageous to make b very large by increasing the thickness of the silver film, it must not be so large that I_0 , the intensity of the light transmitted, is too small.

Let us now consider the light which is incident upon the plates not to be more realistic, but to consist of two wavelengths λ and $\lambda + d\lambda$, then the screen is the focal plane where is covered with two plates of calc spar crystals. The

where Δ is the distance between the plates, λ is the wavelength of the light, n is the refractive index of the medium between the plates.

$$\frac{\Delta}{\lambda} = \frac{1}{2} + \frac{1}{2} \cos \theta$$

where θ is the angle of observation, or

$$d\lambda = \frac{n\lambda^2}{\Delta} \cos \theta$$

Since Δ is always large relative to $n\lambda$, we can write

$$d\lambda = \frac{n\lambda^2}{\Delta} \cos \theta$$

Thus, the spacing of the first order fringes of the spectrum ($\theta = 1$) near the center of the system where θ is so small that $\cos \theta \approx 1$ is given by $d\lambda = \frac{n\lambda^2}{\Delta}$. Knowing the value of λ , and the refractive index, the value of $d\lambda$ can be determined with a very high degree of accuracy. When $d\lambda$ is very small it is not necessary for the determination of its value to separate the plates until the

first order fringes occur, but only till the separation of the fringes is clearly visible. When the separation of the fringes is, say, one quarter of the distance between consecutive fringes of the same radiation, the separation between

$$d\lambda = \frac{n\lambda^2}{\Delta}$$

is very small, and it is not of dependence on the separation between the plates as long as the fringes are visible. The same is true for the other orders of the spectrum.

the central result is correct. It is a consequence of the fact that the path difference between the two rays is zero. The path difference between the two rays is zero at the centre of the pattern. This can be shown if we consider the geometry of the radii of the rings. With the centre of the lens as a bright ring

$$\Delta = 2 D \sin \theta = m \lambda,$$

where m is an integer; for the first bright fringe out from the centre the difference of path is

$$2 D \cos \theta = (m - 1) \lambda,$$

hence, $\tan \theta = \frac{\sqrt{2 D \cos \theta}}{m - 1}$

and the radius R_1 of the ring is given by the expression

$$R_1 = f \tan \theta = f \frac{\sqrt{2 D \cos \theta}}{m - 1}$$

Similarly for the second bright fringe

$$2 D \cos \theta = (m - 2) \lambda$$

hence, $R_2 = f \frac{\sqrt{2 D \cos \theta}}{m - 2}$

and so forth for R_3, R_4 , etc.

The following table gives the values of $R_1/f, R_2/f, R_3/f, R_4/f, R_5/f$ for different values of m .

m	R_1/f	R_2/f	R_3/f	R_4/f	R_5/f
1	∞				
2	1.732	∞			
3	1.316	1.316	∞		
4	1.000	1.000	1.000	∞	
5	0.766	0.766	0.766	0.766	∞

From this table we see that when $m = 1$, i. e., the difference of path is one wave-length, there is only one interference band and its radius is infinite, thus the field would be uniformly illuminated. When the difference of path is two wave-lengths there are only two fringes, the first whose radius is 1.732 f , the radius of the second being infinite. For $m = 3$ there are three fringes. The entire system of bands could only be observed by means of infinite glass plates. We also see that as m gets large, which in practice is generally the case, the lower row in the table shows us that the distance between the first and second ring is much larger than that between the second and third and so on moving out in the system. Thus the separation of the fringes gradually diminished as we go out from the centre, and hence the advantage of making the observations on the central fringes. This is clearly shown by the figures on the plates which are reproduced from photographs.

This interference method, besides being applied for the analysis of spectrum lines, can be used in the study of the changes in the wave-length of any radiation under the different conditions as indicated above. Any small change will be shown by an increase or decrease in the diameters of these rings, and since very clear photographs can be taken, very accurate measurements on the changes produced can be obtained.

APPARATUS.

After experimenting some time with an instrument which seemed to be particularly sensitive to vibrations, even when every precaution was taken to eliminate extraneous disturbances, a new instrument was constructed. In the construction of this instrument the essential parts sought after were, that the mountings for the plates should be rigid and placed on a massive base so that the bands should be perfectly steady, and that the movable carriage carrying one plate should be capable of very slow uniform motion always remaining parallel to its original position, enabling one to follow clearly the change from one band to another.

In working with a Michelson interferometer as made by Gaertner & Co. the fringes obtained were very steady, even when the instrument rested on a table in the laboratory. I took this instrument stripped it of its mirrors and plates, and using the base, carriage, and screw constructed the apparatus employed.

The apparatus consists of two plane glass plates 3.90 c. s. by 2.5 c. s. and about .6cm. thick, each slightly prismatic in shape; the two faces making with one another an angle between 1" and 2". This prevents the interference bands from in the plates themselves being superimposed upon those under

observation. Rotations are rigidly mounted in brass frames. One frame can be moved about a vertical axis and the other about a horizontal axis. For very small motions about these axes, so that the silvered surfaces may be made perfectly parallel, two glass tubes were bent into convenient shapes and clamped to the instrument. Their ends resting against a frame are covered with thin sheet rubber. To the other ends are attached long rubber tubes and these connected with a support. By carefully raising or lowering these tubes, which are filled with mercury, the pressure against the frame being thereby varied, very small rotations around either axis are obtained and the surfaces thereby placed in perfect adjustment. Fabry and Perot employed this method using water in their tubes instead of mercury. The carriage containing one of the frames rests upon steel ways, very accurately ground, and is connected by means of a small carriage, placed underneath, to a screw of 1 mm. pitch. The force being thus applied to the carriage in a direction parallel to the motion produces no rocking, as is shown by the fact that the frames always remained in adjustment during the motion.

To turn the screw two handles are on the instrument, one for rapid and the other for slow motion. A turn of the first corresponds to one turn of the screw. The other is a tangent screw by which it is possible to slide the carriage and in

slow motion that the distance from one fringe to the next can be easily followed. The two mirrors were attached graduated disks enabling the distance between the plates to be accurately known.

The whole instrument weighed over 15 kilograms and was placed on a brick pier. The greater part of the observations were taken at night. With this instrument the fringes were always perfectly steady and very long photographic exposures could be made without the least fear of obtaining a blurred image.

Since the radiations from all the sources studied consisted of many wave-lengths it was necessary to employ some arrangement by which the wave-length under consideration could be separated from the others. The following, Fig. 1, was the plan first adopted. S is the source of light. The radiation undergoes an analysis by a Steinheil spectroscope consisting of two flint-glass prisms. The lens L brings the different wave-lengths to a focus on a screen I, which contains a slit. Through this slit the wave-length considered is allowed to pass and passing between the silvered plates forms the interference bands, which are observed by a telescope T or photographed.

The photographic apparatus consisted of a long light-proof box with a circular hole cut in one side. The eyepiece

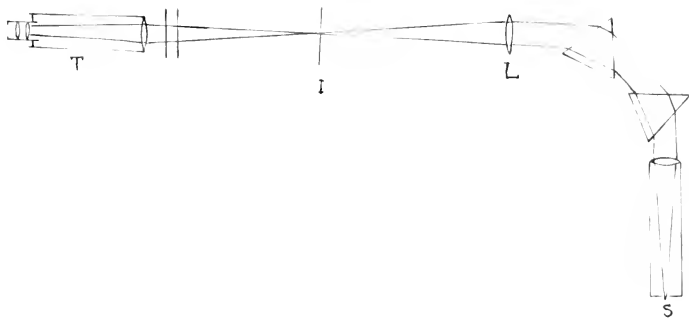


Fig. 2.

of the telescope being received, the plate was placed so that the light was fitted over the end of the telescope. The photographic plate 13 by 3 cms. was in the focus of the objective and mounted so that it could be slid past the opening, and hence a number of exposures made upon one plate.

With the silvered plates illuminated in this way, with divergent light, the entire rings of the interference-bands are observed in the focal plane of the objective as shown on Plate I, fig. 1. The following method, however, was found to be better for the analysis of the radiations. The lens L was removed and the interferometer placed directly behind the prisms so that the parallel light fell upon the silvered plates. With a broad slit in the spectroscopic we have in the telescope, focussed for infinity, broad lines corresponding to the lines in the spectrum. These lines are crossed with the interference-bands produced by the plates. By this means the light has been concentrated into a few interference-bands and on this account many of the weaker components appear which cannot be seen with the light divergent as above. Plate I, fig. 2 shows clearly. This is a photograph of the violet-green mercury radiation as shown in two components when the interference plates are separated 3 mm.

The diameter of the plates is 1.5 cm. and the distance between them is 0.5 cm. The telescope at the same time is turned in such a way that the different kinds of interference-bands depending upon the distribution of the radiation nature is one line. This facilitates greatly the analysis of the radiations and we see at once any change that may take place in one or all of the lines for any change of external conditions. The dispersion of the prisms and the magnification of the telescope were such that about half of the spectrum was visible at once. Plate I, figs. 3, 4 and 5 each show the interference-bands due to the two yellow and green lines of mercury vapour taken at the same time with the plates separated at different distances. On account of the broad slit the yellow lines passed through the interference-plates together and hence their interference-bands are superimposed upon one another. The other lines in this region of the spectrum of mercury being of less intensity do not show in the photographs, which were exposed only long enough to get the clearest pictures of the lines considered. The dark green line was quite visible to the eye after passing through the silvered plates. The curvature of the bands in the different lines is of course due to the amount of separation of the plates and to the angle of incidence which is

* The readings are taken at equal angles of interference-plates.
For the determination of the zero-reading corresponds to the position where the silver plates were in contact, a red or yellow or incandescent sodium vapour in a vacuum-tube was employed. The slit of the spectro-scope being wide the two lines were superimposed so that the two radiations together entered the interferometer. The plates were separated until the first coincidence happened, and the readings taken; the operation was repeated several times. Since the difference, $d\lambda$, between the sodium lines is known with accuracy from Rowland's tables the distance D between the plates can be calculated from the above equation and thus the zero point obtained. Readings were taken of the successive coincidences as the plates were separated and in this manner the screw was calibrated. If a more accurate calibration is required the two yellow lines of mercury can be used; since their distance apart is about three times that of the sodium lines, the coincidences occur three times more often in a given distance.

Remarks on Interference-Plates.

Before considering the results I will add a few remarks concerning the general character of the interference-plates, and the influence of the position of the plates on the results.

When the silvered surfaces are not parallel, if they are tilted to one another at a small angle, the fringes of interference are localized in the plates and, as is well known, can be seen by the eye or with a lens focussed on the plates. These fringes, however, can only be obtained when the separation of the plates is very small.

In order to procure clear interference-bands with great differences of path it is necessary to have the surfaces rigidly parallel. The fringes in this case are seen by the eye, or by means of a telescope focussed for infinity. One of the most important results of this work is that the silvered faces of the plates must be perfectly parallel, and the telescope must be focussed for finity to obtain correct results. While this has been noted by former investigators I wish to strongly emphasize the necessity for these adjustments for if these two conditions are not fulfilled all manner of anomalous results may be expected.

On Plate I are shown some photographs of some of the results obtained, if these conditions are not obeyed. Figs. 6 - 12 were all taken with the bright green line of incandescent mercury vapour in a vacuum-tube. None of the photographs are identified, the focal length of the objective used was about 10 in.

The separation of the interference-plates in figs. 1, 6 and 7 was 3 mm. If, where the adjustments are perfect, 6 and 7 show the effect upon the bands when the interference-plates are only a very small degree from being parallel, they refer displaced from parallelism by merely raising one of the mercury adjusting tubes less than a centimetre.

In figs. 8 and 9 the plates are separated 0.5mm., in neither case are the plates parallel, in 8 they have an angular separation of over 1". These photographs also show the interference-bands produced in the plates themselves superimposed upon the other.

It is to advantage in the observations to obtain all the light possible, thus a broad source is always employed. The interfering rays from the different points of the source can only produce a clear interference pattern in the focal plane of the objective; in any other plane the bright interference-bands will be wide and fuzzy.

Figs. 10, 11, and 12, illustrate this point. The whole slit is covered with the exception of two points separated 4 mm. from one another in a horizontal direction. Fig. 10 shows the effect when the object-plate is placed about 1 cm. inside the focus of the objective. Fig. 11 when the plate is placed 1 cm. beyond the focus. Fig. 12 when the plate is exactly in the focal plane, then the interference

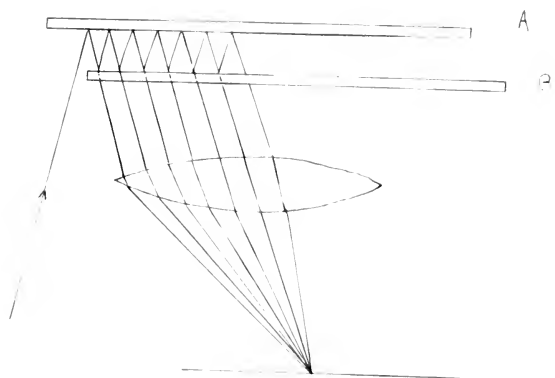


Fig 3.

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RESULTS.

On the basis of what has preceded the following results have been obtained. A number of sources were employed, - metallic vapours in vacuum-tubes rendered luminous by the electric discharge from a large induction-coil, metallic vapours in a Geissler tube and in an electric arc, and lastly the electric spark between electrodes of the metals. This latter source was found to be very unsatisfactory. Of the many sources tried the bright radiation from mercury vapour was the best for obtaining observations on the changes produced in the compounds by external changes in the conditions. We will thus first consider the results with this source. Care pains were always taken to have perfect adjustments chiefly with respect to the focussing of the telescope and the parallelism of the interference-plates, before any readings were taken.

The vacuum-tube discharge was obtained in a Geissler tube with mercury electrodes of the form suggested by Runge and Paschen*, the capillary of which was placed directly in front of the slit of the spectroscop. The different tubes were connected to a Geryk pump and a pressure gauge, enabling the pressure of the vapour to be varied within limits.

* *A. Rep. Phys. Chem.* 10, 123, 1901.

in which the λ is usually λ_0 from a few millimetres to a fraction of a millimetre.

It is rather difficult to decide whether it is the most advantageous way to record results, whether to take λ at all, as the wave-length of gravity of the various components constituting the radiation as the position from which to measure wave-lengths, which is the usual way in the measurements of the lines obtained by means of the grating, or to consider the component of the greatest intensity as the standard and record the wave-lengths of the other components with reference to this; the method is the one employed by Michelson, Fabry and Perot. The latter method, nevertheless, is unsatisfactory, for I have found, even in some of the few radiations investigated, that there are two or more bright components whose intensities are equal. For want of a satisfactory standard, and also that the following results may be easily compared with those of the other investigators, their method has, however, been followed. In the cases where the brightest components are of equal intensity one of them has been selected for the standard. In what follows the plus sign indicates that the component has a longer wave-length than the standard, the minus sign the reverse.

The following results were obtained after a large number of observations with the wave-lengthary λ_0 .

component and the other at a wave-length of 1.5×10^{-4} cm. The radiation was of wave-length 1.5×10^{-4} cm. The two components having about equal intensity, the one having the longer wave-lengths will be considered a standard. The other components have the following differences in wave-lengths and in intensity relative to the one selected.

1.	Standard Component,	Intensity	1
2.	$- 1.1 \times 10^{-4}$ cm.,	"	$3/4$
3.	$- .9$ "	"	$1/4$
4.	$- 0.4$ "	"	1
5.	$+ 0.1$ "	"	$1/8$
6.	$+ 0.4$ "	"	$1/4$

Thus there are three components on the side toward the shorter wave-lengths and two towards the longer.

The violet line, 4353, is a triple having slight components on each side of the principal.

1.	Standard Component,	Intensity	1.
2.	$- 0.5 \times 10^{-4}$ cm.,	"	$1/4$
3.	$+ 0.1$ "	"	$1/4$

Not the yellow lines have numerous components but they are of very slight intensity so that concordant results were not obtained.

When a small amount of air was allowed to enter the vacuum-tube till the pressure was about 5 mm. the intensity of the spectral fringes completely disappeared, the brighter components broadened and their edges became less sharply defined, showing that the atomic vibrations were not so uniform and simple as before. The same effect was noticed with the radiation from a vacuum-tube which had been used some time without any change of pressure. In the case where the pressure is changed through the introduction of air the molecular collisions may be made more frequent, which would naturally interfere with the free vibrations of the atomic systems and so produce a broadening of the bands and cause the less intense fringes to disappear. In the case of an old tube, when the pressure has not changed, there seems to be no other explanation for the observations than that the mercury vapour had become contaminated with gases driven off from the glass by the heat developed in the discharge.

Whether the atomic vibrations in a source are changed on account of the presence of molecules of foreign matter is a open question. Michelson* thinks that the presence of other molecules does not have any appreciable effect except to diminish the visibility. In the case of mercury he con-

* Phil. Mag. 34, 246, 1893.

in [redacted] quite different visibility curves were [redacted] the curve was [redacted] to that obtained when the pressure was low. When the mercury was placed in an atmosphere of hydrogen the characteristics of the visibility curves were not changed. My results show, however, that when mercury is placed in the presence of air both in the vacuum-tube discharge and in the arc, which will be described later, the appearance of the interference-bands is clearly changed, which can only be due to a change in the oscillations of the atomic systems. Schuster in a lecture at the Royal Institution in 1881 drew from his results the conclusion "Placing a molecule in an atmosphere of a different nature - without change of temperature - produces the same effect as would be observed in lowering the temperature". In a note to the *Astrophysical Journal** he says "Something similar seems to take place as regards pressure for the sodium lines may be obtained wide or narrow according as the atmosphere producing the pressure consists of sodium molecules only or of molecules of a different nature". The results here obtained seem to corroborate those of Schuster.

As being of some importance in this subject I have

* *Astrophys. Journ.* 3, 292, 1890.

Fig. 12 is a photograph of the sodium lines, separated and superimposed, obtained with a sodium flame in air as the source. With sodium in a vacuum-tube these bands are as sharp as those of the mercury fringes on Plate I. Fig. 13 was obtained with the green radiation from mercury in a tube which had been used a considerable time. The separation of the plates was 6 mm. Here not even one component is visible. A comparison of this photograph with that of Fabry and Perot reproduced in the *Astrophysical Journal*, May, 1901 may interest the reader. This reproduction is of the fringes of the same line with the same separation of plates but shows the components. The figs. 13, 14, 15, Plate II have been magnified about five times. Fig. 16 has not been magnified, and shows how sharp the bands are when the plates are separated 1 cm. Here also the components of the mercury green radiation are invisible.

With tubes containing capillaries whose diameters are greater than 2 mm. the light obtained with an ordinary discharge is not sufficiently intense to show the finer components. The components that can be seen have their edges quite sharp, showing that the vibrations in these tubes are probably the same as in the tubes of smaller capillaries. The finer the capillary the greater the electrical resistance to the discharge and hence a rise in the temperature, causing a

ultra violet. Temperature is an important factor, for on heating only the capillary of the tube was hot there is no liquid mercury present and thus producing no noticeable change in the pressure in the vacuum tube, the kinetic energy of the electrons is increased such that many of the components of small intensity invisible before are now very readily seen.

The number and intensity of the components were the same whether the tube was placed "side on" or "end on", that is whether the discharge was perpendicular or parallel to the propagation of the light through the slit.

The introduction of capacity in parallel with the discharge circuit had no interesting effect. With three parallel jars, each gallon jars, the fringes were broadened and the finer components disappeared. The effect appeared in every way analogous to that when the pressure was increased.

The next step was to investigate the radiations from a mercury arc and compare the results with the one alone. After many trials with different kinds of arcs the following form, fig. 1, was found to be most satisfactory. The arc is between two mercury surfaces. A very ordinary glass receiver of about 60 cc. capacity, over the front B is placed a piece of plate glass; a red glass window stopper C is used to fill

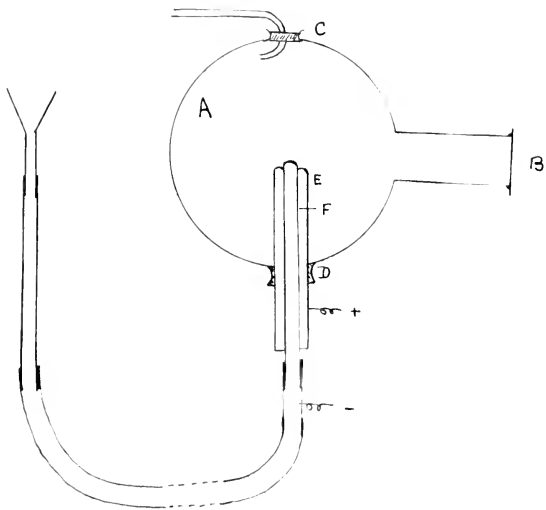


Fig 4.

the arc is produced by a battery (D) connected to the electrodes. The diameter of the arc is 13 mm., and the whole of it is enclosed in a porcelain tube of diameter 19 mm. This porcelain tube is connected with a glass tube which in turn is connected with a large rubber tube. The space between the porcelain and glass tubes as well as the porcelain, glass, and rubber tubes attached. The electric poles are placed as shown in the figure. By raising the mercury column until a drop of mercury flows over into E the arc is started. Any further adjustments are easily carried out by raising or lowering the mercury column. Since all the joints were made air-tight the pressure could be varied by means of the pump. Within a few seconds after the arc is started the whole bulb of receiver is covered with a layer of mercury thrown off from the arc, this does not penetrate into the neck so that the glass at C is always clear and the radiation from the arc passes through to the slit of the spectroscope without loss. The whole apparatus is placed in a cold water bath to keep the joints cool. This was found unnecessary with the apparatus used even when the arc was steadily run for ten minutes. Generally 150 volts were employed, the current was varied by means of a rheostat, generally 1 ampere was used.

With this pressure under which the experiments were made, as those obtained with vacuum-tubes as given above. Above this pressure it was very difficult to obtain any components and the bands were broad and fuzzy. This is probably due, as above, to pressure and the presence of a number of molecules of air.

The results obtained with the other metallic vapours and gases are briefly as follows.

Cadmium. Small pieces of metallic cadmium were enclosed in a Geissler tube surrounded by an asbestos jacket; when heated with a Bunsen flame the metal easily vaporized.

The red line 6439 is nearly monochromatic; there is, however, a weak component towards the shorter wave-lengths.

1.	Standard Component,	Intensity	1
2.	- 0.1×10^{-8} mm.,	"	$1/5$

The green line 5086 is composed of four components the three weaker being on the side towards the larger wave-lengths.

1.	Standard Component,	Intensity	1.
2.	+ 0.4×10^{-8} mm.,	"	$1/4$
3.	+ 0.25 "	"	$1/4$
4.	+ 0.1 "	"	$1/5$

The blue line 4700 has a component on the longer side

principal.

1.	Standard Component,	Intensity	1.
2.	+ 0.6×10^{-8} mm.,	"	1/3
3.	- 0.4 " "	"	1/4

Thallium. A piece of metallic thallium was placed on the end of a platinum wire and held in a Bunsen flame. The only bright radiation was that of the green line, 5329. A doubling of bands occurred when the plates were separated only a few millimetres. With a vacuum-tube radiation, another component was found with wave-length between the principal and first component.

1.	Standard Component,	Intensity	1.
2.	+ 1.0×10^{-8} mm.	"	3/4
3.	+ 0.4 " "	"	1/4

Hydrogen. By the kindness of Dr. Parsons I used one of his tubes containing hydrogen which was specially pure, the pressure being 1 mm. The red line easily breaks up into three components one on each side of the brightest component.

1.	Standard Component,	Intensity.	1
2.	+ 0.6×10^{-8} mm.,	"	1/4
3.	- 0.2×11 " "	"	1/3

The green line is very complex, the components are so numerous that observations are very difficult.

The values in the components are the same in pressure, size of capillary, capacity in circuit which were obtained principally with the mercury radiations were in some cases tested with other radiations considered and the results were in general the same. The above results with respect to the relative wave-length and intensity of the components under the conditions specified are collected in the following table together with the results of Michelson, and Fabry and Perot upon the same radiations obtained in vacuum-tubes. Michelson's values are taken from the curves given in his paper. His method does not allow the determination as to whether the components have longer or shorter wave-lengths than the standard. The second list of values for the components of the mercury line, $\lambda = 5461$, obtained by Fabry and Perot are taken from a paper by Zeeman.

After the many long and tedious observations together with the study and elimination of the errors which may enter into the results due to imperfect adjustments of the apparatus, the author regrets that he is unable to present a more detailed account of the variations that occur in these component radiations or satellites as they have been called. The changes occur so suddenly on the least change of the surrounding conditions and sometimes even when no change

Observation.		Approx. Error.		Alt. or	
Latitude	Intensity.	Latitude	Intensity.	Altitude	Intensity.

Mercury, $\lambda = 4353$					
1. Std. Comp.	1	1. Std. Comp.	1	1. Std. Comp.	1
2. - 1.1	1/10	2. - 0.9	1/6	2. - 1.1	1/4
3. - 1.6	1/4	3. - 0.1	1/3	3. - 0.9	1/4
4. - 0.7	1/10	4. - 0.1	1/4	4. - 0.1	1
5. - 0.1		5. - 0.1	1/4	5. - 0.1	1/4
6. - 0.1		6. - 0.1	1/4	6. - 0.1	1/4
7. + 1.3		7. + 1.3	1/4	7. + 1.3	1/4

Mercury, $\lambda = 4353$

1. Std. Comp.	1	1. Std. Comp.	1
2. - 1.1	1/10	2. - 1.1	1/4
3. - 1.6		3. - 1.6	1/4

Mercury, $\lambda = 4353$

1. Std. Comp.	1	1. Std. Comp.	1
2. - 1.1	1/10	2. - 1.1	1/4

Mercury, $\lambda = 4353$

1. Std. Comp.	1	1. Std. Comp.	1	1. Std. Comp.	1
2. - 1.1	1/10	2. - 1.1	1/4	2. - 1.1	1/4
3. - 1.6		3. - 1.6	1/4	3. - 1.6	1/4
4. - 0.7		4. - 0.7	1/4	4. - 0.7	1/4
5. - 0.1		5. - 0.1	1/4	5. - 0.1	1/4
6. - 0.1		6. - 0.1	1/4	6. - 0.1	1/4
7. + 1.3		7. + 1.3	1/4	7. + 1.3	1/4

$\lambda = 0$		$\lambda = 1$		$\lambda = 2$	
1. 1.0	1	1. 1.0	1	1. 1.0	1
2. 1.0	1/2	2. 1.0	1/2	2. 1.0	1/2
3. 1.0	1/2	3. 1.0	1/2	3. 1.0	1/2

Median, $\lambda = 0.50$

1. 1.0	1	1. 1.0	1	1. 1.0	1
2. 1.0	1/2	2. 1.0	1/2	2. 1.0	1/2
3. 1.0	1/2	3. 1.0	1/2	3. 1.0	1/2

Mean, $\lambda = 0.50$

1. 1.0	1	1. 1.0	1	1. 1.0	1
2. 1.0	1/2	2. 1.0	1/2	2. 1.0	1/2
3. 1.0	1/2	3. 1.0	1/2	3. 1.0	1/2
4. 1.0	1/2	4. 1.0	1/2	4. 1.0	1/2

Median, $\lambda = 1.00$

1. 1.0	1	1. 1.0	1	1. 1.0	1
2. 1.0	1/2	2. 1.0	1/2	2. 1.0	1/2
3. 1.0	1/2	3. 1.0	1/2	3. 1.0	1/2

different to the observer were introduced, that only qualitative results of a very general nature can be expressed.

During the observations upon the sharp interference-fringes due to the mercury green radiation in the two cases, when the components were visible as exemplified by the photograph given by Fabry and Perot as referred to above, and when with the same separation of the silvered plates, the components were not present as exemplified by Fig. 13, Plate II, the question arose, - was the change in the conditions given birth to one or more satellites? The sharpness of the fringes in both cases, the unequal change in the intensity of the various components under various conditions, as is shown when the capillary of a vacuum-tube is heated, and in the fact that the results given in the above table upon the distances between the components are in good agreement which is probably due to the different circumstances surrounding the radiation, all point to the possibility of the production of satellites. It must not be forgotten, however, that at the separation of the plates necessary to show the presence of the components the interference-fringes are very close to one another so that it is impossible in this method for an interference-fringe due to the birth of a satellite to appear without overlapping some part of the in-

reference-fringe of the interference pattern would provide a new distribution of light in the interference-pattern which would naturally lead to different results.

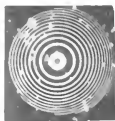
The investigations of the variations in the wave-length and intensity of radiations separated by the grating on account of variation in pressure, electrical condition of the discharge, and the chemical nature of the dielectric surrounding the luminous substance, is at present a very fruitful field. For these changes in these widely separated lines lend themselves to measurement. It is hoped that a method will be found which will more readily show and give measurements of the many changes that occur in radiations whose wave-lengths and hence their frequencies do not differ greatly, so that ultimately some knowledge as to the mechanics of the systems of moving electrons constituting the atom whose periods differ by small amounts relative to those obtainable at present may be obtained. A step in this direction has been made by Lummer. The reproductions in the *Ann. d. Phys.*, 10, p. 173, 1903, show excellently the complicated structure of these bright radiations. The method proposed above, employing lens plates is worthy of a fair trial.

My earliest thanks are due to my professors and to my friends at this university, especially Professor [Name], who, along with my fellow students, whose assistance in word and deed has greatly facilitated these experiments.

Physical Laboratory,

Johns Hopkins University.

Plate I.



1.



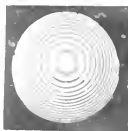
2.



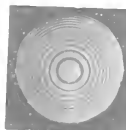
3

4.

5.



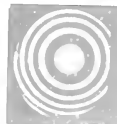
6.



7



8



9.



10.



11.



12.

Interference fringes under various conditions

Plate II

13.



14.



15.

16.

Figs. 13 and 16 green in original
Figs. 14 and 15, sodium lines.

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λ

λ

λ

λ

The first part of the paper discusses the importance of the parameter λ in the context of the model. It is shown that the value of λ can significantly affect the results of the analysis. The second part of the paper presents the results of the analysis, which are compared with the results of previous studies. The third part of the paper discusses the implications of the results for the theory and practice of the field.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100

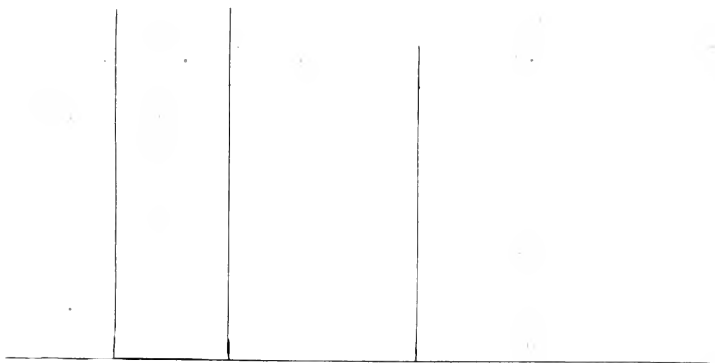
λ

60 c. 15.

1. 1.



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λ

λ

spark
↑

λ

λ

λ

λ

λ

λ

λ

λ

Plate III

- Spectrum of
Magnesium Arc
obtained in a Vacuum.

1.

⋮
λ 4481

Spectrum showing line λ 4481
only at the cathode.

λ 4481
⋮
⋮

2.

—

